Self-optimizing Concurrency in Software
Transactional Memory via Model-based Approach

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Abstract

In the era of multi-core systems, the need for tools simplifying the development of concurrent applications is increasingly looming. In such a context, Software Transactional Memory (STM) is recognized as an effective programming paradigm, thanks to its ability to guarantee consistency of data that are shared across concurrent threads in an application transparent manner. On the other hand, a core problem to cope with for STM, which has received great attention of late, deals with (dynamically) regulating the degree of concurrency, in order to deliver optimal performance. In fact, depending on the application workload, whose profile can also change over time, an oversized number of concurrent threads may cause loss in performance due to excessive data contention, which may give rise to excessively high transaction abort rate. Conversely, an undersized number of threads may hamper performance due to limited exploitation of parallelism. We address this problem by proposing a self-regulation approach of the concurrency level, which leverages a parametric analytical performance model aimed at predicting the scalability of the STM application as a function of the actual workload profile and the number of concurrent threads supposed to sustaining the execution. The regulation scheme allows achieving optimal performance during the whole lifetime of the application via dynamically resizing the number of concurrent threads according to the predictions by the model. The later is customized for a specific application/platform pair through regression analysis, which is based on a lightweight sampling phase. We also present a real implementation of the model-based concurrency self-regulation architecture integrated within the open source TinySTM framework. Further, the effectiveness of the proposal is evaluated via an experimental assessment based on standard STM benchmark applications.

Keywords: Software Transactional Memory, performance modeling, concurrency regulation, self-tuning

The software produced as a result of the research activity presented in this paper can be downloaded at the URL http://www.dis.uniroma1.it/~hpdcsl/CSR-STM.tar
I. INTRODUCTION

Software Transactional Memory (STM) [1] has emerged as a promising paradigm that aims at simplifying the development of parallel/concurrent applications. Leveraging on the well know concept of atomic transaction, STM provides application developers with a friendly alternative to traditional lock-based synchronization. More in detail, any code block accessing data that are shared across concurrent threads can be marked as a transaction, thus demanding coherency of the data access/manipulation to the STM layer, rather than to any handcrafted synchronization scheme. The relevance of the STM paradigm has significantly grown given that multi-core systems have become mainstream computing platforms, so that even entry-level desktop and laptop machines are nowadays equipped with multiple processors and/or CPU-cores.

Even though one main target for STM is the simplification of the software development process, another aspect that is central for the success of the STM paradigm relates to the actual level of performance it can deliver. As for this aspect, STM needs to be complemented by schemes aimed at determining the well suited degree of concurrency (in terms of number of threads exploited for running the application), which is expected to allow the overlying application to reach optimal speedup values thanks to fruitful parallelism exploitation. This issue arises since STM applications are prone to thrashing phenomena (caused by excessive transactions rollbacks) in case the data access pattern tends to exhibit non-negligible conflict among concurrent transactions and the degree of parallelism in the execution is excessively high. On the other hand, for too low parallelism levels, the achievable speedup may still be suboptimal.

Recent approaches coping with this problem have been targeted at selecting/controlling the degree of parallelism by (dynamically) determining the well suited number of concurrent threads to sustain application execution. Such a suited concurrency level is expected to lead to the exploitation available computing resources (namely the available CPU-cores) at the maximum extend still avoiding thrashing phenomena, hence optimizing the achievable speedup. Along this path we can find solutions ranging from analytical models [2], [3], to heuristic-based schemes [4], to machine learning approaches [5]. On the other hand, any of the proposed approaches exhibits some shortcoming. Classical analytical approaches are in fact know to become unreliable as soon as the assumptions they rely on (e.g. in terms of data access distribution and/or distribution of the CPU time for specific operations) are not met. Further, according to the outcomes in [6], the transaction abort rate can be strongly affected by the order according to which data are accessed along the transaction execution path, which is typically neglected by analytical models. On the other hand, even in case the effects of such an ordering are captured analytically, the actual exploitation of the performance model would require detailed knowledge of the data access pattern for the specific application, which may be unavailable or arduous to build. As for heuristic and/or machine learning approaches, they do not require specific (stringent) assumptions to be met in relation to, e.g., the transactional profile of the application. Hence,
they exhibit the potential for high effectiveness in generic application contexts, and for generic computing platforms. On the other hand, these approaches entail limited extrapolation capabilities, thus being unsuited for forecasting the performance that would be achieved with levels of concurrency not belonging to the already explored domain (e.g. the training domain in case of machine learning). Further, the time required for building the knowledge base to be exploited by the machine learner may be non-minimal, which may make the actuation of the optimized concurrency configuration untimely.

In this article we tackle the issue of regulating the concurrency level in STM via a model-based approach, which differentiates from classical ones in that it avoids the need for the STM system to meet specific assumptions (e.g. in terms of data access pattern). Our proposal relies a parametric analytical expression capturing the expected trend in the transaction abort probability (versus the degree of concurrency) as a function of variations of a set of features associated with the actual workload profile. The parameters appearing within the model exactly aim at capturing execution dynamics and effects that are hard to be expressed through classical (non-parametric) analytical modeling approaches. We derived the parametric expression of the transaction abort probability via combined exploitation of literature results in the field of analytical modeling and a simulation-based analysis. Further, the parametric model is thought to be easily customizable for a specific STM system by calculating the values to be assigned to the parameters (hence by instantiating the parameters) via regression analysis. The latter can be performed by exploiting a set of sampling data gathered through run-time observations of the STM application. However, differently from what happens for the training process in machine learning approaches, the actual sampling phase (needed to provide the knowledge base for regression in our approach) is very light. Specifically, a very limited number of profiling samples, related to a few different concurrency levels for the STM system, likely suffice for successful instantiation of the model parameters via regression. Finally, our approach inherits the extrapolation capabilities proper of pure analytical models (although it does not require their typical stringent assumptions to be met, as already pointed out), hence allowing reliable performance forecast even for concurrency levels standing distant from the ones for which sampling was actuated.

A bunch of experimental results achieved by running the STAMP benchmark suite [7] on top of the TinySTM open source framework [8] are reported for validating the proposed modeling approach. Further, we present the implementation of a concurrency self-regulating STM, exploiting the proposed model-based approach, still relying on TinySTM as the core STM layer, and we report experimental data for an assessment of this architecture.

The remainder of this paper is organized as follows. In Section II, literature results related to our proposal are discussed. Section III is devoted to describing and validating our STM performance model. The STM architecture entailing self-regulation capabilities of the concurrency level is presented and evaluated in Section IV.
Our proposal has relations with literature results in the field of analytical modeling of concurrency control protocols for transactional systems. These include performance models for traditional database systems and related concurrency control mechanisms (see, e.g., [9], [10], [11]) and approaches specifically targeting STM (see, e.g., [12]). One common point for literature analytical models is that they either rely on (stringent) assumptions on the data access pattern or rely on the knowledge of the precise distribution of the accesses performed by the transactions. The first category includes models (see, e.g., [11], [13]) that assume data to be uniformly accessed on one or more datasets of fixed cardinality. In [9] the b-c model is assumed, where b% of the transactions are assumed to uniformly access elements within the c% of the dataset, and the remaining accesses are assumed to be targeted to the remaining data. This model has been further extended in [14], [15], in order to encompass several transactional classes, each accessing a disjoint portion of the whole dataset. Differently from all these works, our proposal does not assume any specific distribution for the data accesses, thus being more general and exploitable in generic application contexts. This is achieved by relying on a parametric analytical expression (as opposed to non-parametric models) where one role of the parameters is exactly to avoid the need for explicitly expressing hard-to-capture dynamics and effects related to the specific data access pattern exhibited by the transactional application.

The second category includes models which are able to capture more complex data access patterns (see, e.g., [16], [6]), such as when assuming a different probability to access a set of data depending on the phase of execution of the transaction (which is expressed via a matrix representation where an element m(i,j) specifies the probability for a transaction to access datum j at operation i). Compared to these solutions, our proposal avoids the need for any detailed characterization of the data access distribution. As a reflection of this aspect, the instantiation of the parameters appearing in our model requires a much lighter application sampling process than what required to instantiate the actual data access distribution (e.g. in terms of m(i,j) values) to be provided in input to the aforementioned models.

In [17] the authors propose a technique to approximate the performance of the STM application when considering different amounts of concurrent threads. The technique is based on the usage of different types of functions, such as polynomial, rational and logarithmic functions. The approximation process relies on sampling the speed-up of the application over a set of runs, each one executed with a different number of concurrent threads. After, the speed-up forecasting function is instantiated by interpolating the measurements. Compared to our proposal, a limitation of this approach lies on that the workload profile of the application is not taken into account while instantiating the performance forecasting function. This may lead to reduced reliability of the forecasting outcome, especially when the sampled application changes its workload profile.

As for machine learning, it has been used in [18] in order to select the best performing conflict detection and management algorithm. Conversely, it has been used in [19] to select suitable thread to CPU-core mappings allowing
performance improvements thanks to increased effectiveness of the caching system. The goal of both these works is different and orthogonal with respect to our one since we focus on the regulation of the overall concurrency level in the system. To the best of our knowledge, the only machine learning based approach targeting this same problem has been presented in [5]. Compared to this solution, the present proposal relies on a sampling process that is lighter than the one required for building the machine learning based performance model via training. Further, the approach in [5] suffers from limited extrapolation capabilities (in terms of ability to forecast speed-up values for concurrency levels that are outside the training domain), as typical of machine learning (as confirmed by experimental data we report in this paper). Instead, the present proposal entails high extrapolation capabilities, being it based on an analytical approach.

The work in [4] presents a black-box approach, based on the hill-climbing heuristic scheme, which dynamically increases or decreases the level of concurrency within the STM. Particularly, the approach determines whether the trend of increasing/decreasing the concurrency level has positive effects of the observed throughput, in which case the trend is maintained. Differently from our proposal, no direct attempt to capture the relation between the actual transaction profile and the achievable performance (depending on the level of parallelism) is done. Further, similarly to the case of machine learning based schemes, the proposal in [4] does not entail significant extrapolation capabilities.

Given that our model-based approach is ultimately aimed at regulating concurrency to the optimal level, for which thrashing phenomena do not appear, our proposal is related to pro-active transaction scheduling schemes, which cope with the issue of performance degradation due to excessive data contention [20], [21], [22]. These solutions avoid scheduling the execution of transactions whose associated conflict probability is estimated to be high. The work in [20] presents a control algorithm that dynamically changes the number of threads concurrently executing transactions on the basis of the observed transaction conflict rate. It is decreased when the rate exceeds a threshold while it is incremented when the rate is lower than another threshold. In [21], incoming transactions are enqueued and sequentialized when an indicator, referred to as contention-intensity, exceeds a pre-determined threshold. The contention intensity is calculated as a dynamic average depending on the number of aborted vs committed transactions. In the approach in [22], a transaction is sequentialized when a potential conflict with other running transactions is predicted. The prediction leverages on the estimation of the expected transaction read-set and write-set (on the basis of the past behavior of others or the same transaction). The sequentializing mechanism is activated only when the amount of aborted vs committed transactions exceeds a given threshold. Compared to our model-based concurrency regulation approach, all the above proposals do not directly estimate the likelihood of transaction aborts as a function of the level of concurrency. Rather, they attempt to control the wasted time in an indirect manner according to heuristics schemes.
As already hinted, we decided to exploit a model leveraging a parametric analytical expression which captures the expected trend of the transaction abort probability while varying: (1) a set of features characterizing the current workload profile, and (2) the number of concurrent threads sustaining the STM application. The parameters of the analytical expression aim at capturing effects that are hard to express through a classical (non-parametric) analytical modeling approach. Further, they are exploited to customize the model for a specific STM application through regression analysis, which is done by exploiting a set of sampling data gathered through run-time observations of the application. In the remainder of this section we provide the basic assumptions on the behavior of the STM application, which are exploited while building the parametric analytical model. Then the actual construction of the model is presented. Finally, the outcomes of a model validation study, carried out with STM benchmark applications specified by STAMP [7], are reported.

A. Basic Assumptions

The STM application is assumed to be run on top of a number $k$ of concurrent threads. The execution flow of each thread is characterized by the interleaving of transactions and non-transactional code ($ntc$) blocks. This is the typical structure for common STM applications, which is also reflected in most of the widely diffused STM benchmarks (see, e.g., [7]).

The read-set (write-set) of a transaction is the set of shared data objects that are read (written) by the thread while executing the transaction. If a conflict between two concurrent transactions occurs, then one of the conflicting transactions is aborted and re-started (which leads to a new transaction run). After the thread commits a transaction, it executes a $ntc$ block, which ends before the execution of the begin operation of the subsequent transaction along the same thread.

B. Model Construction

The set of features $P$ exploited for the construction of the parametric analytical model, which are used to capture the workload profile, consists of:

- the average size of the transaction read-set $rs_s$;
- the average size of the transaction write-set $ws_s$;
- the average execution time $t_t$ of committed transaction runs (i.e. the average duration of transaction runs that are not aborted);
- the average execution time $t_{ntc}$ of $ntc$ code-blocks;
• the read/write affinity \(rw_a\), namely the probability that an object read by a transaction is also written by other transactions;

• the write/write affinity \(ww_a\), namely the probability that an object written by a transaction is also written by other transactions.

Operatively, \(rw_a\) can be calculated as the dot product between the distribution of read operations and the distribution of write operations (both expressed in terms of relative frequency of accesses to shared data objects). On the other hand, \(ww_a\) can be calculating as the dot product between the distribution of write operations and itself.

Our parametric analytical model expresses the transaction abort probability \(P_a\) as a function of the parameters belonging to the set \(P\), and the number \(k\) of concurrent threads supposed to run the STM application. Overall, it expresses (in a parametric manner) the structure of the function:

\[
p_a = f(rs_s, ws_s, rw_a, ww_a, t_t, t_ntc, k)
\]  

(1)

Leveraging literature results, particularly literature models proposing approximated performance analysis for transaction processing systems (see [11], [23]), we capture the expected trend for the transaction abort probability through the function

\[
p_a = 1 - e^{-\alpha}
\]  

(2)

However, while in literature results the parameter \(\alpha\) is expressed as the multiplication of parameters directly expressing, e.g. the data access pattern and the workload intensity (such as the transaction arrival rate \(\lambda\) for the case of open systems), in our approach we express \(\alpha\) as the multiplication of different functions, which in their turn depend on the set of input parameters appearing in Equation (1). Overall, our expression for \(p_a\) is structured as follows

\[
p_a = 1 - e^{-\rho \omega \phi}
\]  

(3)

where the function \(\rho\) is assumed to depend on the input parameters \(rs_s, ws_s, rw_a\) and \(ww_a\), the function \(\omega\) is assumed to depend on the parameter \(k\), and the function \(\phi\) is assumed to depend on the parameters \(t_t\) and \(ntc_t\).

As an important preliminary observation, Equation (2) has been derived in literature while modeling the abort probability for the case optimistic concurrency control schemes, where transactions are aborted (and restarted) right upon detecting any conflict. Consequently, this expression for \(p_a\) and the variation we propose in Equation (3) are both expected to well match the STM context, where pessimistic concurrency control schemes (according to which transactions can experience lengthy lock-wait phases upon conflicting) are not used since they would limit the exploitation of parallelism in the underlying architecture. More specifically, in typical STM implementations (see, e.g., [8]), transactions are immediately aborted right upon executing an invalid read operation. Further, they are aborted on write-lock conflicts either immediately or after a very short wait-time.
The model we propose in Equation (3) is parametric thanks to expressing $\alpha$ as the multiplication parametric functions that depend on a simple and concise representation of the workload profile (via the features in the set $P$) and on the level of parallelism. This provides it with the ability to capture variations of the abort probability (e.g. vs the degree of parallelism) for differentiated application profiles. Particularly, different applications may exhibit similar values for the featuring parameters in the set $P$, but may anyhow exhibit different dynamics, leading to a different curve for $p_a$ while varying the degree of parallelism. This is catchable by our model vis application-specific instantiation of the parameters characterizing the functions $\rho$, $\omega$ and $\phi$, which can be done through a simple regression-analysis process. In the next section we discuss how we have derived the actual $\rho$, $\omega$ and $\phi$ functions, hence the actual function expressing $\alpha = \rho \cdot \omega \cdot \phi$.

C. Instantiating $\rho$, $\omega$ and $\phi$

The shape of the functions $\rho$, $\omega$ and $\phi$ determining $\alpha$ is derived in our approach by exploiting the results of a simulation study. We decided to exploit simulation, rather than using measurements from real systems, since our model is aimed at capturing the effects associated with data contention on the abort probability, while it is not targeted at capturing the effects of thread-contention on hardware resources (such as shared interconnections and/or shared lower level caches on a multi-core machine). Consequently, the instantiation of the functions appearing within the model has been based on an ”ideal hardware” simulation model showing no contention effects due to concurrency. Anyway, when exploiting our data contention model for concurrency regulation in a real system, a hardware scalability model (e.g. a queuing network-based model) can be used to estimate variations of the processing time due to contention effects on shared hardware resources as a function of the number of the concurrent threads. In the final part of this paper, we provide some results that have been achieved by exactly using our data contention model and a very simple hardware scalability model in a joint fashion, with the target of regulating at run-time the STM concurrency level to performance suited values.

The simulation framework we have exploited in this study is the same used in [3] for validating a traditional analytical performance model for STM. Details on this simulation framework are provided in the Appendix. In the simulation runs we performed to derive and validate the expression of $\alpha$, we varied $r_{ss}$ and $w_{ss}$ between 0 and 200, $rw_a$ and $ww_a$ between $25 \cdot 10^{-6}$ and 0.01, $t_t$ between 10 and 150 $\mu$sec, and $t_{ntc}$ between 0 and $15 \cdot 10^4$ $\mu$sec. These intervals include values that are typical for the execution of STM benchmarks such as [7], hence being representative of workload features that can be expected in real execution contexts. Further, we varied $k$ between 2 and 64 in the simulations. Due to space constraints, we omit to explicitly show all the achieved simulation results. However, the shown results are a significant, although concise, representation of the wider set of all achieved results.

The building of the analytical expressions for $\rho$, $\omega$ and $\phi$ has been based on an incremental approach, where we step-by-step validate the incrementally achieved expression of $p_a$. Particularly, we first derive the expression of $\rho$
analyzing simulation results varying workload configuration parameters affecting it, i.e. \(rs_s, ws_s, rw_a, ww_a\), while keeping fixed other parameters. After, we calculate the values of \(\rho\) from the ones achieved for \(pa\) via simulation, which is done by using the inverse function \(\rho = f^{-1}(pa)\), once set \(\omega = 1\) and \(\phi = 1\). After having identified a parametric fitting function for \(\rho\), we derive the expression of \(\omega\) via the analysis of the simulation results achieved while also varying \(k\). Hence, we calculate \(\omega = f^{-1}(pa)\), where we use for \(\rho\) the previously identified expression, and where we set \(\phi = 1\). Therefore, we select a parametric fitting function for \(\omega\). Finally, we use the same approach to derive the expression of \(\phi\), which is done by exploiting the simulation results achieved while varying all workload profile parameters and the level of concurrency \(k\), thus calculating \(\phi = f^{-1}(pa)\), where we use for \(\rho\) and \(\omega\) the previously chosen expressions.

In order to derive the expression of \(\rho\), we initially analyzed via simulation the relation between the values of \(pa\) and the values of the parameters \(ws_s\) and \(ww_a\). In Figure 1 we provide some results showing the values of \(\rho\) as calculated through the \(f^{-1}(pa)\) inverse function (like depicted above) by relying on simulation data as the input. Particularly, the data refer to variations of \(ww_a\) and to 3 different values of \(ws_s\), while all the other parameters have been kept fixed. We note that \(\rho\) appears to have a logarithmic form. Additionally, in order to chose a parametric function fitting the calculated values of \(\rho\), we need to consider that if \(ww_a = 0\) then \(pa = 0\). In fact, no data contention ever arise in case of no write operations within the transactional profile (which implies \(\rho = 0\)). Thus, we approximated the dependency of \(\rho\) on \(ww_a\) through the following parametric logarithmic function:

\[
c \cdot \ln(a \cdot ww_a + 1)
\]

where \(a\) and \(c\) are the fitting parameters. We note that the presence of the \(+1\) term in the above expression is due to the above-mentioned constraint according to which \(ww_a = 0\) implies \(\rho = 0\).

After, we also considered the effects of the parameter \(ws_s\) on \(\rho\). To this aim, in Figure 2 we report the values of \(\rho\), derived from the simulation results, while varying \(ws_s\) and for 3 different values of \(ww_a\). We remark the presence of a flex point. Therefore, in this case, we approximated the dependency of \(\rho\) on \(ws_s\) using the function:

\[
e \cdot (\ln(b \cdot ws_s + 1))^d
\]

where \(b\), \(d\) and \(e\) are fitting parameters. The flex is captured by the above expression through the presence of the parameter \(d\). Assuming that the effects on the transaction abort probability are multiplicative with respect to \(ww_a\) and \(ws_s\) (which is aligned to what literature models state in term of the proportionality of the abort probability wrt the multiplication of the conflict probability and the number of operations, see, e.g., [11]), we achieved the following parametric expression of \(\rho\) (vs \(ww_a\) and \(ws_s\)), where \(d\) has been used as the exponent also for expression in (4) in order to capture the effects of shifts of the flex point caused by variations of \(ww_a\) (as shown by the plots in Figure 2 relying on simulation):

\[
[c \cdot (\ln(b \cdot ws_s + 1)) \cdot \ln(a \cdot ww_a + 1)]^d
\]
where we collapsed the original parameters $c$ and $e$ within one single parameter $c$. We validated the accuracy of
the function in expression (6) via comparison with values achieved through a set of simulations, where we used
different workload profile parameters. On the other hand, the parameters appearing in expression (6) have been
calculated through regression analysis. Specifically, for each test, we based the regression analysis on 40 randomly
selected workload profiles achieved while varying $ww_a$ and $ws_s$. Then, we measured the average error between
the transaction abort probability evaluated via simulation and the one predicted using for $\rho$ the function in expression (6)
for a set of 80 randomly selected workload profiles. As an example, in Figure 6, we depict results for the case with
$k = 8$. Along the x-axis, workload profiles are identify by integer numbers (id) and are ordered by the associated
values of $ws_s$ and $ww_a$. The average error we measured in all the performed tests was 5.3%.

Successively, we considered the effects on the transaction abort probability caused by read operations. Thus,
we analyzed the relation between $p_a$ and the parameters $rs_s, rw_a$ and $ws_s$. The parameter $ws_s$ is included since
contention on transactional read operations is affected by the amount of write operations by concurrent transactions.
In Figure 4 we report simulation results showing the values of $\rho$ while varying $rs_s$ and for 3 different values of $rw_a$.
In Figure 5, we report values of $\rho$ achieved while varying $rw_a$ and for 3 different values of $rs_s$. We note that the
shape of the curves are similar to the above cases, where we analyzed the relation between $p_a$ and the parameters
$ww_a$ and $ws_s$. Thus, using a similar approach, and considering that $p_a$ is also proportional to $ws_s$, we approximate
the dependency of $\rho$ on $rw_a$, $ws_s$ and $ww_a$ using the following function:

$$[e \cdot (\ln(f \cdot rw_a + 1)) \cdot \ln(g \cdot rs_s + 1) \cdot ws_s]^z$$

(7)

where $e$, $f$, $g$ and $z$ are the fitting parameters. The final expression for $\rho$, including the dependencies on all the relevant
parameters, is, in our model, the sum of the expressions (6) and (7). Intuitively, this is related to that adding read
operations within a transaction, the likelihood of abort due to conflicts on original write operations does not change.
However, the added read operations give rise to an increase of the overall abort probability for the transaction, which
we capture summing the two expressions. Also in this case, we validated the final expression for $\rho$ via comparison
with the values achieved through a set of simulations, where we varied the workload profile. Similarly to what done
before, the regression analysis has been based on 40 workload profiles, while the comparison has been based on
80 workload profiles, all selected by randomly varying $ww_a$, $ws_s$, $ws_a$, $rs_s$. The results for $k = 8$ are reported in
Figure 6. Along the x-axis, workload profiles are ordered by values of $rs_s$, $rw_a$, $ws_s$ and $ww_a$. The average error
we measured in all the tests was 2.7%.

Successively, in order to build the expression for $\omega$, we considered the effects of the number of concurrent threads,
namely the parameter $k$, on the abort probability. On the basis of simulation results, some of which are reported in
Figure 7, we decided also in this case to use a parametric logarithmic function as the approximation curve of $\omega$ vs
$k$. Clearly, the constraint needs to be accounter for that if $k = 1$ then $\omega = 0$ (since no concurrency cannot give rise
to transaction aborts. Thus, we approximate \( \omega \) as:

\[
\omega \approx h \cdot (ln(l \cdot (k - 1) + 1),
\]

(8)

where \( h \) and \( l \) are the fitting parameters. Again, we validated the out-coming function for \( p_a \), depending on \( \omega \) (and hence depending on modeled effects of the variation of \( k \)), using the same amount of workload profiles as in the previous studies, still selected by randomly varying \( w_{wa}, ws_s, rw_{wa}, rs_s \) and \( k \). Some results are depicted in Figure
Fig. 4: Variation of $\rho$ with respect to read-write affinity

Fig. 5: Variation of $\rho$ with respect to read-set size

Fig. 6: Comparison between transaction abort probability measured and predicted while varying $rw_a$, $rs_s$, $ww_a$ and $ws_s$
Fig. 7: Variation of ω with respect to the number of concurrent threads

Fig. 8: Comparison between transaction abort probability measured and predicted while varying k, rw_a, rs_s, w_w_a and ws_s

Finally, we built the expression of φ, which depends on t_t and t_ntc. To this aim, we note that if t_t = 0 (which represent the unreal case where transactions are executed instantaneously) then φ must be equal to 0 (give that the likelihood of concurrent transactions is zero). Additionally, we note that t_t can be seen as the duration of a vulnerability window during which the transaction is subject to be aborted. For longer fractions of time during which transaction are vulnerable, higher probability of actual transaction aborts can be expected. Thus we assume φ to be proportional to

$$\theta = \frac{t_t}{t_t + t_{ntc}},$$  

(9)

We analyzed through simulations the relation between φ and θ. Some results are shown in Figure 9, on the basis of which we decided to approximate φ using the function:

$$m \cdot \ln(n \cdot \theta + 1)$$  

(10)

where m and n are the fitting parameters.
Fig. 9: Variation of $\phi$ with respect to $\theta$

Fig. 10: Comparison between transaction abort probability measured and predicted while varying all workload profile parameters

The expression of $p_a$ in Equation (3) is now fully defined. To validate such final expression, we used the same approach that has been adopted for the validation of each of the aforementioned incremental steps. Some results, where we randomly selected workload profiles, are shown in Figure 10. In all our tests, we measured an average relative error of 4.8%.

D. Model Validation with Respect to a Real System

As a further validation step we compared the output by the proposed model with real measurements taken by running applications belonging to the STAMP benchmark suite [7] on top of the open source TinySTM framework [8]. Additionally, we evaluated the model ability to provide accurate predictions while varying the amount of samples used to perform the regression analysis, gathered through observations of the behavior of the real system. Particularly, we evaluate the extrapolation capability of the model, namely its ability to forecast the transaction abort probability that would be achieved when running the STM application at levels of concurrency levels (number of of threads) not included in the observed domain, where regression samples are taken.
The presented results refer to three different benchmark applications of the STAMP suite, namely Kmeans, Yada and Vacation. As shown in [7], these three applications are characterized by quite different workload profiles, in terms of various parameters, such as the transaction duration, read-set and write-set sizes, data access distribution, ratio between the time spent executing transactions and the total application execution time. This allowed us to evaluate the model accuracy with respect to a relatively wide workload configuration domain. All the tests have been performed on top of an HP ProLiant server equipped with two AMD OpteronTM6128 Series Processor, each one having eight CPU-cores (for a total of 16 cores), and 32 GB RAM, running Linux Debian with kernel version 2.7.32-5-amd64.

For each application, we performed regression analysis to calculate three different sets of values for the model parameters, hence instantiating three models relying on the proposed parametric analysis. Any regression has been performed using one of three different sets of measurements, each set including 80 samples. The first set included samples gathered observing the application running with 2 and 4 concurrent threads. The second one included samples gathered observing the application running with 2, 4 and 8 concurrent threads. Finally, the third one included samples gathered observing the application running with 2, 4, 8 and 16 concurrent threads. This allowed us to evaluate the extrapolation ability of the model, with respect the number of concurrent threads, while observing the application for limited amounts of concurrency levels (say for 2, 3 or 4 different levels of concurrency). We performed, for each application, the following tests. After setting up the model instances, we executed a set of runs of the application using different values for the application input parameters (leading the same application to run with somehow different profiles) and with a number of concurrent threads spanning from 2 to 16. During each run, we measured the average values of the workload profile features included in the set $P$ along different observation intervals having a pre-established length, and we used them as the input to the three instantiated models in order to compute the expected abort probability for each observation interval. After, for each instantiated model, we compared the predicted value with the real one observed during the runs.

In Table I, we reported the average value of the prediction error (and its variance) for all the target benchmark applications, and for the three model instances, while considering variations of the actual level of concurrency between 2 and 16. By the results, we note that, for the cases of Yada and Vacation, it has been sufficient to execute regression analysis with samples gathered observing the application running with only 2 and 4 threads in order to achieve a prediction error of 2.4% for any level of concurrency between 2 and 16. When enlarging the observation domain for the gathering of samples to be used by regression, i.e. when observing the application running also with 8 concurrent threads, we achieved for Yada a slight error reduction. With Vacation, the reduction is more accentuated. On the other hand, the prediction error achieved with observations of the application running with 2 and 4 concurrent threads only was noticeably greater for Kmeans with respect to the other applications. However, such an error drastically drops down when including samples gathered with 8 concurrent threads in the data set for regression. As for regression based on samples gathered with 2, 4, 8 and 16 threads, we note that the error marginally increases in all the cases. We
believe that this is due to the high variance of the values of the transaction abort probability we measured along the execution with 16 concurrent threads, which give rise to variability of the results of the regression analysis depending on the set of used observations. Overall, by the results, we achieved good accuracy and effectiveness by the model since it can provide (very) low prediction error, for a relatively wide range of hypothesized thread concurrency levels (namely between 2 and 16) by just relying on observing the application running with 2, 4 and (at worst also) 8 concurrent threads. In fact, for two out of three selected benchmarks, limiting the observations to concurrency levels set to 2 and 4 was sufficient in order to get extremely accurate prediction.

We conclude this section comparing the extrapolation ability of our model with respect the neural network-based model proposed in [5], which, similarly to ours, has been targeted at the estimation of the STM performance (vs the level of concurrency). To perform fair comparison, a same set of observations has been provided to both the models. Particularly, the reported results refer to the Yada benchmark application, for which we provided a set of 80 observations (the same used for validating the model, as shown above), related to executions with 2 and 4 concurrent threads, to both our parametric model and the neural network based model in [5]. As for the neural network approach, we used a back-propagation algorithm [24], and we selected the best trained network, in terms of prediction accuracy, among a set of networks having a number of hidden nodes spanning from 2 and 16, using a number of algorithm iterations spanning from 50 to 1600. In Figure 11, we show two dispersion charts, each one representing the correlation between the measured values of the transaction abort probability and the ones predicted using the model (top chart) and the neural network (bottom chart). These refer to concurrency level spanning in the whole interval 2-16. We remark that a lower prediction error corresponds to a higher concentration of points along the diagonal straight line evidenced in the graphs. We can see that, in the case of the neural network, there is a significantly wider dispersion of points compared to the model we are proposing. In fact, the average prediction error for the neural network is equal to 17.3% while for the model, it is equal to 2.385%. This is a clear indication of higher ability to extrapolate the abort probability by the model when targeting concurrency levels for which no real execution sample is available (and/or that are far from the concurrency levels for which sampling has been actuated). As a reflection, the parametric model we present provides highly reliable estimations, even with a few profiling data available for

<table>
<thead>
<tr>
<th>Application</th>
<th>2 and 4 threads</th>
<th>2, 4 and 8 threads</th>
<th>2, 4, 8 and 16 threads</th>
</tr>
</thead>
<tbody>
<tr>
<td>Vacation</td>
<td>2.166% (0.00089)</td>
<td>1.323% (0.00028)</td>
<td>1.505% (0.00032)</td>
</tr>
<tr>
<td>Kmeans</td>
<td>18.938% (0.09961)</td>
<td>2.086% (0.00100)</td>
<td>2.591% (0.00109)</td>
</tr>
<tr>
<td>Yada</td>
<td>2.385% (0.00029)</td>
<td>2.086% (0.00016)</td>
<td>2.083% (0.00022)</td>
</tr>
</tbody>
</table>

TABLE I: Abort probability prediction error (and its variance)
the instantiation of its parameters. Hence it is suited for the construction of concurrency regulation systems inducing low overhead and providing timely selection of the best suited parallelism configuration (just because the model needs a few samples related to a limited set of configurations in order to deliver its reliable prediction on the optimal concurrency level to be adopted). The organization of an effective concurrency self-regulation architecture exactly exploiting the parametric model is presented and experimentally assessed in the next section.
IV. CONCURRENCY SELF-REGULATING STM

A. The Architecture

The architecture of the Concurrency Self-Regulating STM (CSR-STM) is depicted in Figure 12. A Statistic Collector (SC) provides a Control Algorithm (CA) with the average values of workload profile parameters, i.e. $r_s$, $w_s$, $r_w$, $w_w$, $t_t$ and $t_{ntc}$, measured by observing the application on a periodic basis. Then, the CA exploits these values to calculate, through the parametric model, the transaction abort probability $p_{a,k}$ as predicted when using $k$ concurrent threads, for each $k$ such that $1 \leq k \leq \text{max\_thread}$. The value $\text{max\_thread}$ represents the maximum amount of concurrent threads admitted for executing the application. We remark that a number of concurrent threads larger than the number of available CPU-cores typically penalizes STM performance (e.g. due to costs related to context-switches among the threads [25], as well as cache invalidation and refill costs). Hence, it is generally convenient to bound $\text{max\_thread}$ to the maximum number of available CPU-cores. The set $\{(p_{a,k}), 1 \leq k \leq \text{max\_thread}\}$ of predictions is used by the CA to estimate the number $m$ of concurrent threads which is expected to maximize the application throughput. Particularly, $m$ is identified as the value of $k$ for which

$$\frac{k}{w_{time,k} + t_{t,k} + t_{ntc,k}}$$

is maximized. In the above expression: $w_{time,k}$ is the average transaction wasted time (i.e. the average execution time spent for all the aborted runs of a transaction) when the application is supposed to run with $k$ concurrent threads; $t_{time,k}$ is the average execution time of committed transaction runs when the application is supposed to run with $k$ concurrent threads; $t_{ntc,k}$ is the average execution time of $ntc$ code-blocks when the application is supposed to run with $k$ concurrent threads.

We note that $w_{time,k} + t_{t,k} + t_{ntc,k}$ is the average execution time between commit operations of two consecutive transactions executed by the same thread when there are $k$ active threads. Hence, the formula in (11) expresses the system throughput. Now we discuss how $w_{time,k}$, $t_{t,k}$ and $t_{ntc,k}$ are estimated. We note that $w_{time,k}$ can be evaluated multiplying the average number of aborted runs of a transaction and the average duration of an aborted transaction run when the application is executed with $k$ concurrent threads. Thus, the average number of aborted transaction runs with $k$ concurrent threads can be estimated as $p_{a,k}/(1 - p_{a,k})$, where $p_{a,k}$ is calculated through the presented model.

To calculate the average duration of an aborted transaction run, as well as to estimate $t_{t,k}$ and $t_{ntc,k}$, while varying $k$, an hardware scalability model has to be used. In the version of CSR-STM we present in this study, we exploited the model proposed in [26], where the function modeling hardware scalability is:

$$C(k) = 1 + p \cdot (k - 1) + q \cdot k \cdot (k - 1)$$
where \( p \) and \( q \) are fitting parameters, and \( C(k) \) is the scaling factor when the application runs with \( k \) concurrent threads. The values of \( p \) and \( q \) are again calculated through regression analysis. Thus, assuming that, e.g., during the last observation interval there were \( x \) concurrent threads and the measured average transaction execution time has been \( t_{t,x} \), then CA can calculate \( t_{t,k} \) for each value of \( k \) through the formula \( t_{t,k} = C(k)/C(x) \cdot t_{t,x} \).

Once estimated the number \( m \) of concurrent threads which is expected to maximize the application throughput, CA keeps active such a number of threads during the subsequent workload sampling interval.

### B. Evaluation Study

In this section we present an experimental assessment of CSR-STM, where we used the benchmark applications mentioned above, namely Vacation, Kmeans and Yada, running on top of the same 32-core HP ProLiant server exploited for previous experiments. All tests we present focus on the comparison of the execution time achieved by running the applications with on top of CSR-STM and on top of the original version of TinySTM. Specifically, in each test, we measured, for both CSR-STM and TinySTM, the delivered application execution times while varying \( \text{max\_thread} \) between 2 and 16. In the case of TinySTM, \( \text{max\_thread} \) corresponds to the (fixed) number of concurrent threads exploited by the application. While, in the case of CSR-STM, the application starts its execution with a number of concurrent thread equal to \( \text{max\_thread} \). However, CSR-STM may lead to changes of the number of concurrent threads setting it to any value between 1 and \( \text{max\_thread} \), selected as the optimal concurrency level.

For each application, we calculated the values of the parameters of the model through a regression analysis where we used samples gathered observing the application running with 2 and 4 concurrent threads for the cases of Vacation and Yada, and including also observations with 8 concurrent threads for the case of Intruder. As for the parameters appearing in the hardware scalability model expressed in (12), regression analysis has been performed by using, for each application, the measured average values of the committed runs of transactions, observed with 2, 4 and 8 concurrent threads. The cost of initial sampling and regression are included in the final execution latency delivered by CSR-STM for fairness in the comparison.

To evaluate the ability of CSR-STM to regulate the concurrency level, we performed a number of runs using, for each application, different values for the input parameters. Due to space constraints, we only report results achieved with two different workload profiles for each application, which are shown in Figures 13, 14 and 15 for Vacation, Kmeans and Yada, respectively. On top of each charts, we report, according to the syntax of the input string established by STAMP, the values of the input parameters that we used to run the application.

Observing the results, the advantages of CSR-STM with respect to TinySTM can be easily appreciated. For system configurations where CSR-STM is allowed to use a maximum number of threads (\( \text{max\_thread} \)) greater then the optimal concurrency level (as identified by the peak performance delivered by TinySTM), it always tunes the concurrency
level to suited values. Thus it avoids the performance loss experienced by TinySTM when making available a number of CPU-cores exceeding the optimal parallelism level. Particularly, the performance by TinySTM tends to constantly degrade while incrementing the parallelism level, according to the increase of the available number of CPU-cores. Conversely, CSR-STM prevents this performance loss, providing a performance level which is, for the majority of the cases, near to the best value, independently of the actual number of available CPU-cores for running the application. Obviously, when $max_{thread}$ is lower then the optimum concurrency level, CSR-STM can not activate the well suited number of concurrent threads, which equals the optimal level of parallelism. However this occurs since the scenario mimics a run in an undersized platform. Thus, for these configurations, the performance of CSR-STM, in some cases, is slightly reduced with respect to TinySTM due to the overhead associated with the components/tasks proper of the concurrency self-regulation mechanism. In relation to these components, we note that, except for the case of the SC, for which we measured a negligible overhead, the other components, i.e., the CA and the model solver, require a single processing thread to be run (mostly residing in wait phases). Thus, their overhead on hardware resources is reduced, with respect to the total application workload, of a factor bounded by $1/k$, when considering $k$ available CPU-cores. In fact, by the results, the cases where CSR-STM provides lower performance than TinySTM (e.g. when $max_{thread}$ is less than 4 for Vacation and Kmeans), the advantage by TinySTM progressively decreases while incrementing $max_{thread}$.

V. Summary

In this article we have presented a parametric analytical model for determining the optimal level of concurrency in STM applications. Application-specific instantiation of the parameters can be actuated via a light regression process based on a few samples related to the run-time behavior of the application. Also, the model does not rely on any strong assumption in relation to the application profile, hence being usable in generic application contexts. It has been validated via comparison of its outcomes with real data traced by running applications from the STAMP benchmark.
suite on top of a 32-core HP ProLiant machine. We also presented a concurrency self-regulation architecture based on the model, which has been integrated in the TinySTM open source framework, and report experimental data showing it can effectively control the concurrency level to values delivering (close to) optimal performance.

VI. APPENDIX: SIMULATION MODEL DETAILS

The simulation model we used is implemented on a discrete-event simulation platform. It simulates a closed system with $k$ concurrent threads, each one alternating the execution of transactions and non-transactional code ($ntc$) blocks. The concurrency control algorithm is the default algorithm of TinySTM (encounter time locking for write operations and timestamp-based read validation). A transaction starts with a `begin` operations, then it interleaves the execution of read/write operations (accessing a set of shared data objects) and local computation phases, and, finally, executes a `commit` operations. Duration of $ntc$ blocks, operations of transactions and local computation phases are distributed exponentially.
REFERENCES


